

Validation of Geant4 fragmentation for Heavy Ion Therapy

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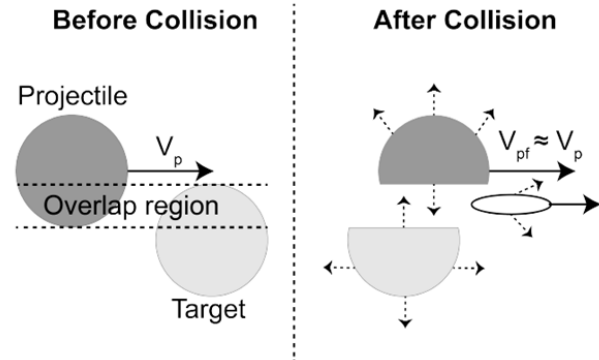
HIT mixed radiation field

Reference:

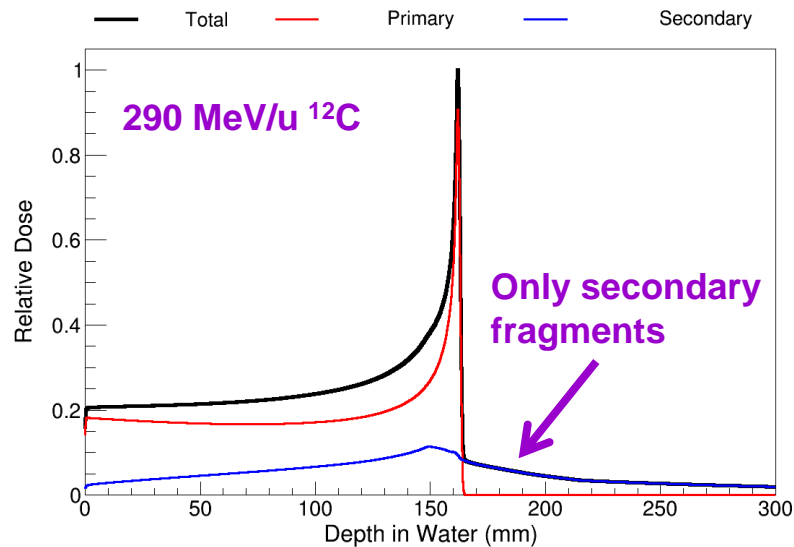
Francis et al, PMB, 59 (2014) 7691

Contribution to the **dose**:

- 64% - ^{12}C ions via em interactions
- 36% - produced fragments and their secondaries
 - 14% - protons
 - 13% - alpha particles
 - 4.2 % - B ions
 - 1.7% - Li ions
 - 1.3% - Be ions

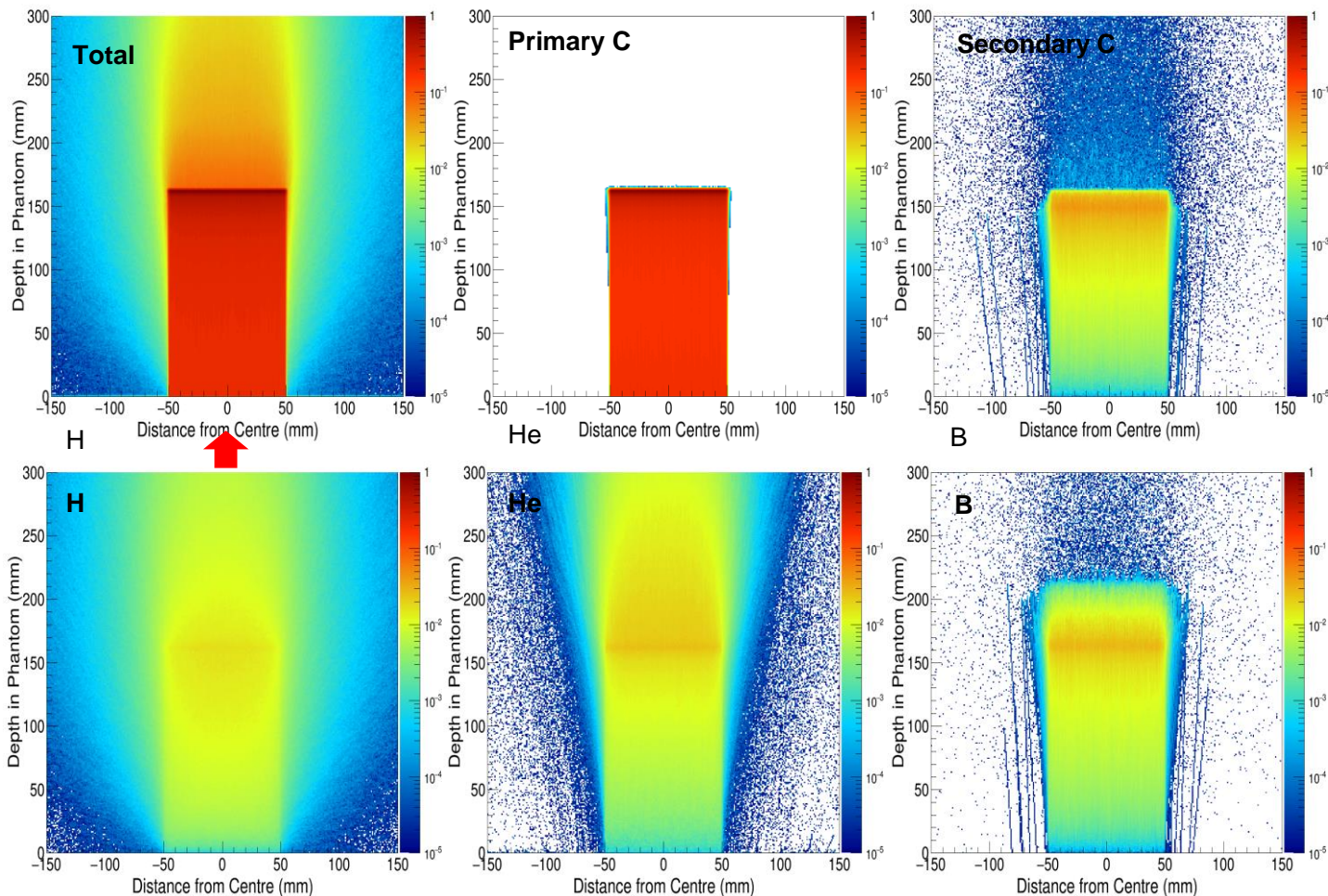


Creation of an excited product which will de-excite by emitting nucleons and smaller fragments (depicted by the dashed arrows).



Dose in the water phantom

290 MeV/u ^{12}C



Experimental Data

- Fragmentation study of a 400MeV/u ^{12}C pencil beam (FWHM 5mm) studied at GSI
- Bragg Curve, fragment yields, angular and energy distribution of fragments

IOP PUBLISHING

PHYSICS IN MEDICINE AND BIOLOGY

Phys. Med. Biol. **58** (2013) 8265–8279

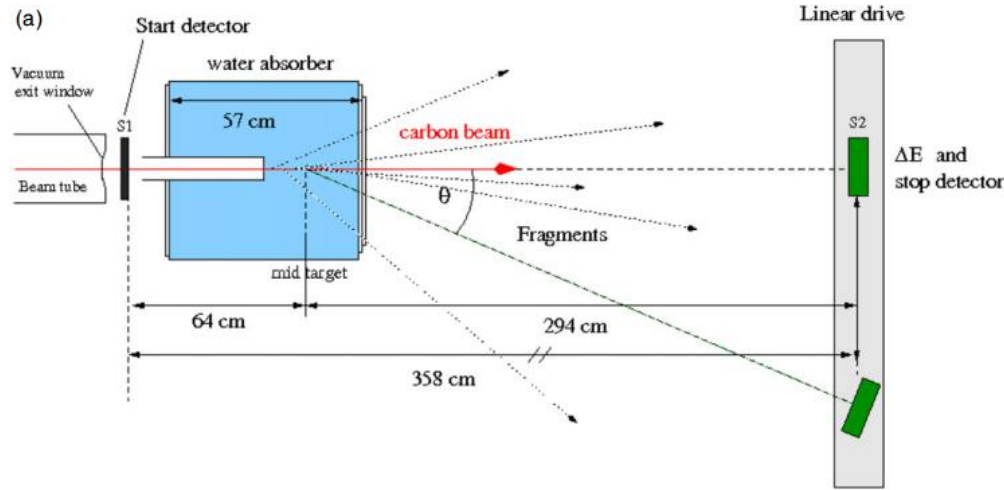
[doi:10.1088/0031-9155/58/23/8265](https://doi.org/10.1088/0031-9155/58/23/8265)

Experimental study of nuclear fragmentation of 200 and 400 MeV/u ^{12}C ions in water for applications in particle therapy

E Haettner, H Iwase¹, M Krämer, G Kraft and D Schardt

GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt, Germany

Experimental reference data



400 MeV/u ^{12}C beam incident upon a water phantom performed at GSI in Germany by Haettner et al. PMB 58 (2013) 8265-8279

The experiment was conducted using a variable thickness water Phantom

Time of flight measurements for fragments were carried out using a start detector and a second detector placed on a linear drive after the phantom

Sketch from PMB 58, (2013), 8265-8279

Previous Work

- Böhlen et al studied BIC and QMD in Geant4 v9.3 and FLUKA

Benchmarking nuclear models of FLUKA and GEANT4 for carbon ion therapy

T T Böhlen^{1,2}, F Cerutti¹, M Dosanjh¹, A Ferrari¹, I Gudowska²,
A Mairani³ and J M Quesada⁴

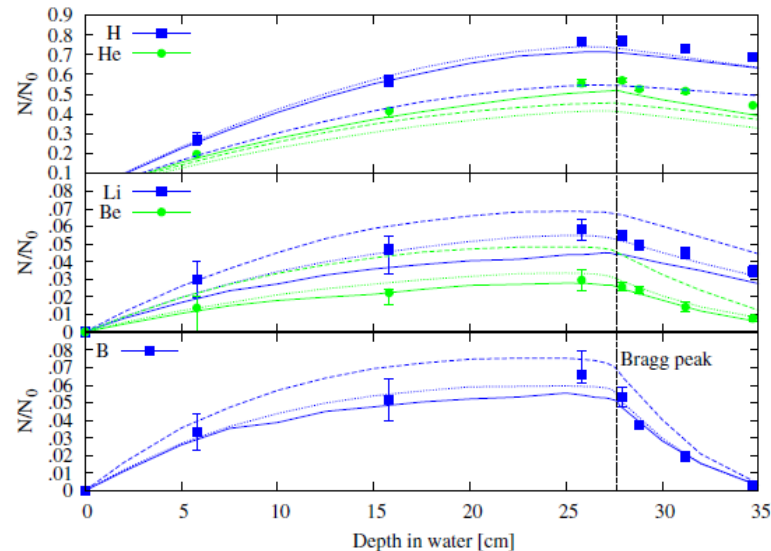
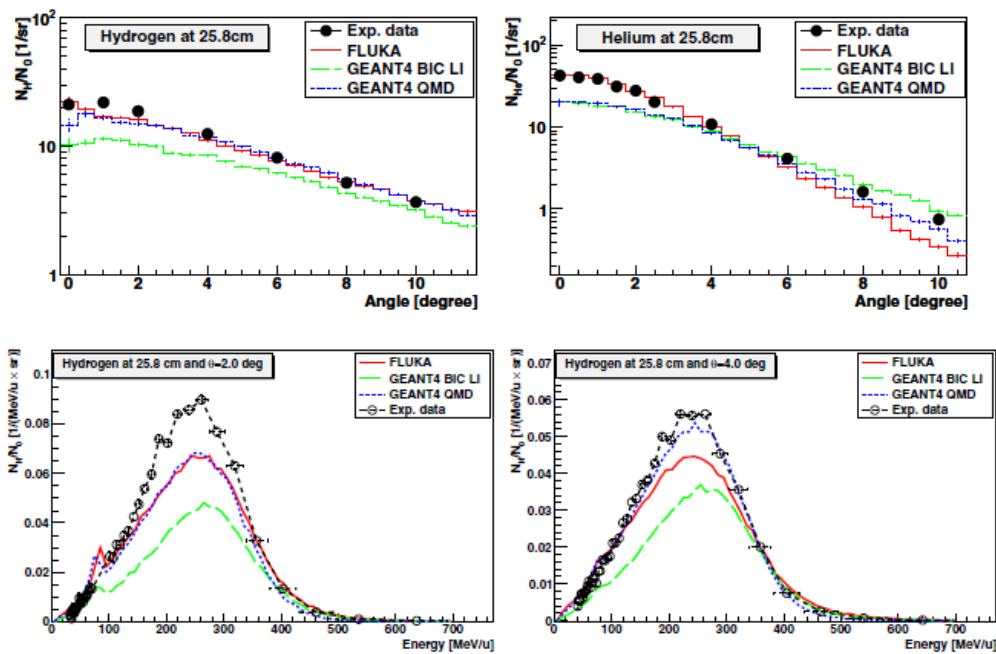
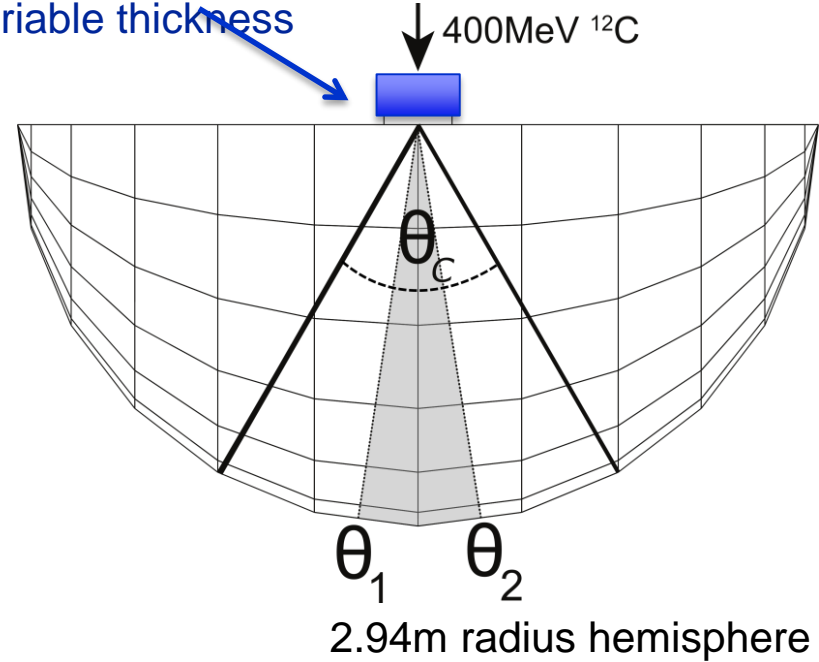


Figure 5. Fragment build-up curves in water of a 400 MeV/u carbon beam as a fraction of primary carbon ions N/N_0 . Experimental data are shown as points (Haettner *et al* 2006). Simulations done for FLUKA (solid) and for GEANT4 using the BIC LI (dashed) and the G4QMD (dotted) model are displayed as lines. The dashed vertical line indicates the position of the Bragg peak.

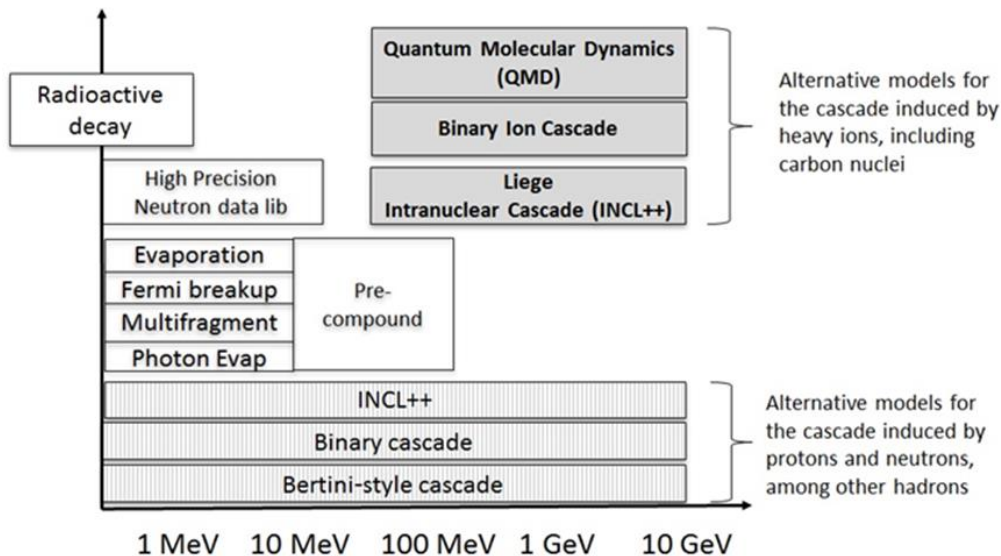
Project Summary

- Quantify the accuracy of different fragmentation models in Geant4 benchmarked for a 400MeV/u ^{12}C beam
 - Fragment yields
 - Angular distributions
 - Kinetic energy distributions of fragments with $Z=1-5$
- Geant4 10.2.patch2
- EMStandardOption3

Water phantom of variable thickness



Geant4 ion cascade models



- **BIC**
 - interaction between a projectile and a single nucleon of the target nucleus interacting in the overlap region as Gaussian wave function
- **QMD and QMD-Frag**
 - all nucleons of the target and projectile, each with their own wave function; greater computation times than BIC
- **INCL**
 - nucleons as a free Fermi gas in a static potential well.
 - Targets and projectiles with $A \leq 18$.

Partial Geant4 hadronic physics inventory
Of interest for carbon ion therapy

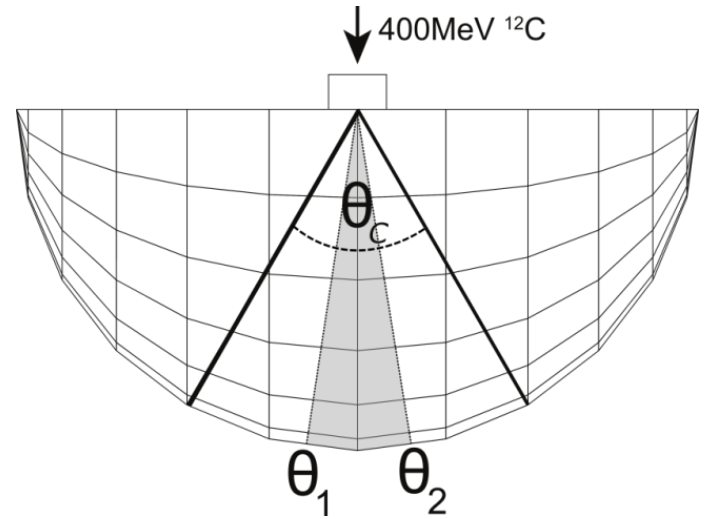
Ranking Models

- To quantify how well each model performs:
 - $\langle PE \rangle$: mean percentage difference

$$\langle PE \rangle = \frac{100}{n} \left(\sum_{i=1}^n \left| \frac{Sim_i - Exp_i}{Exp_i} \right| \right)$$

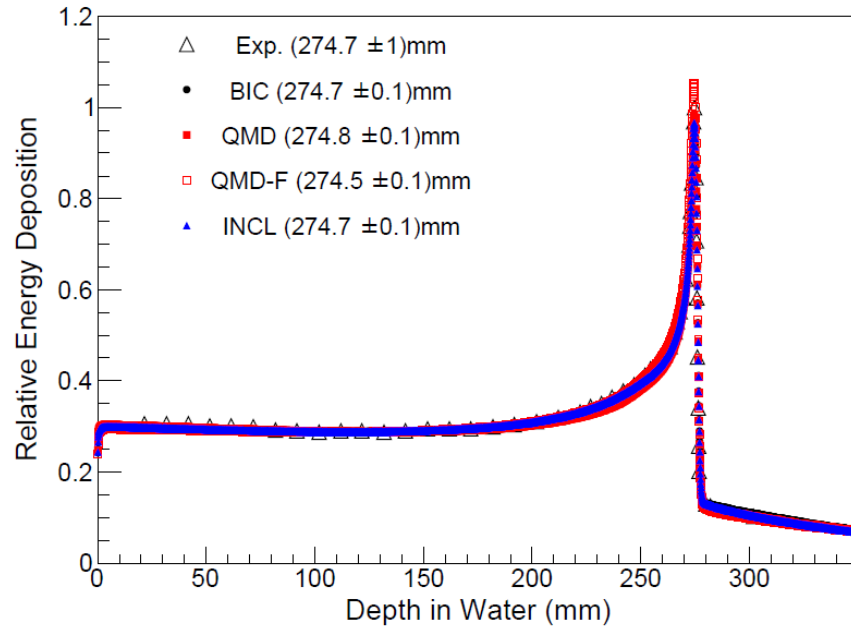
– χ^2

$$\chi^2 = \sum_{i=1}^n \frac{(Sim_i - Exp_i)^2}{Exp_i}$$

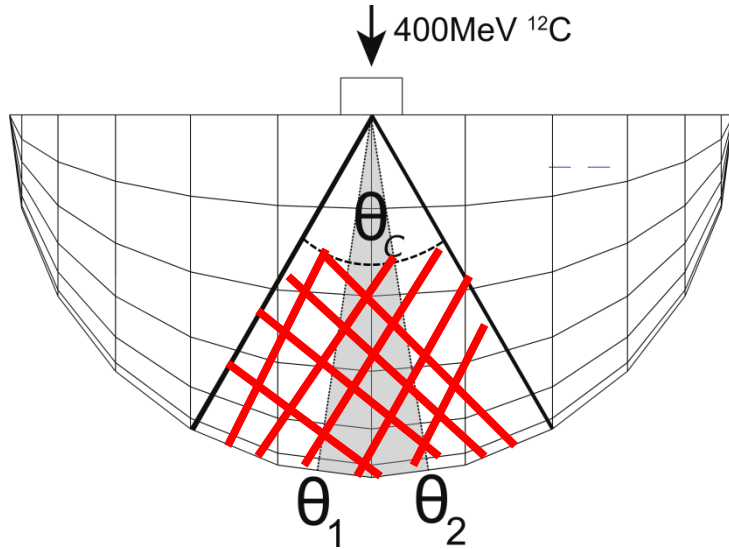


Results: Bragg Peak

- Good agreement with experimental measurements
- QMD-F provides best agreement

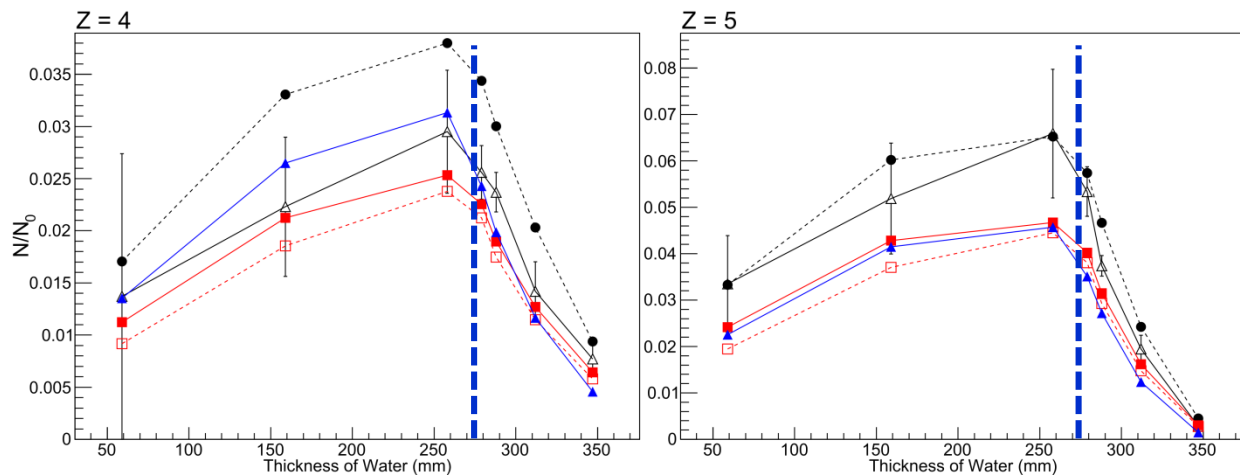
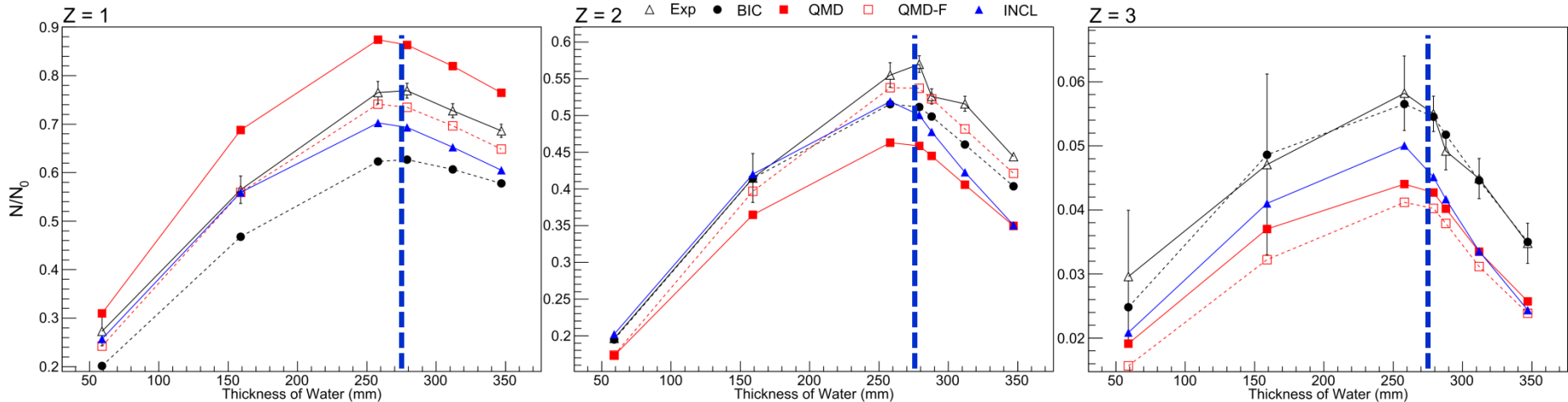


	BIC	QMD	QMD-F	INCL
X^2	53.098	54.335	46.720	52.021



Fragment Yields

Measuring Fragment yield
in 10° cone (θ_c)



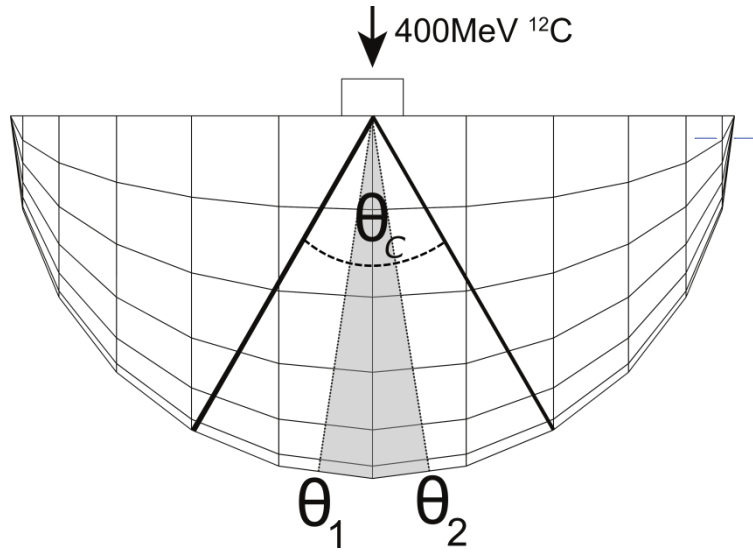
Experimental errors of H and He fragments are $\sim 5\%$,
 for heavier fragments they increase to $\sim 20\%$, before the BP and $\sim 10\%$ After BP

Results: Fragment yields

- Models agree ~5-35% with exp
- QMD-F performed best for lighter fragments

Mean %Difference

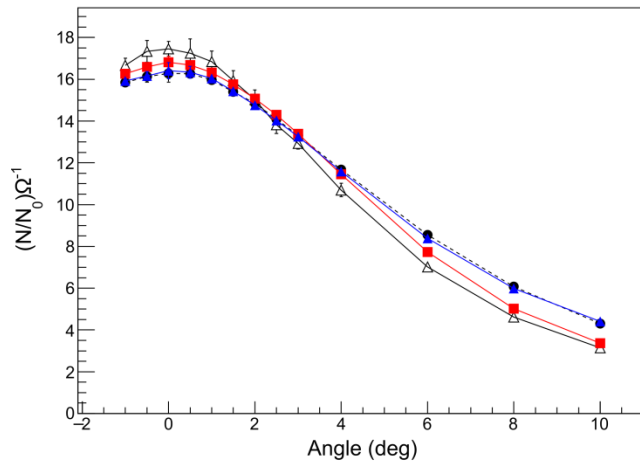
Z	BIC	QMD	QMD-F	INCL
1	19 ± 2	14 ± 2	5 ± 2	8 ± 2
2	6 ± 1	17 ± 1	5 ± 1	10 ± 1
3	4 ± 7	25 ± 7	31 ± 7	21 ± 7
4	32 ± 10	14 ± 10	22 ± 10	15 ± 10
5	19 ± 8	20 ± 8	26 ± 8	33 ± 8



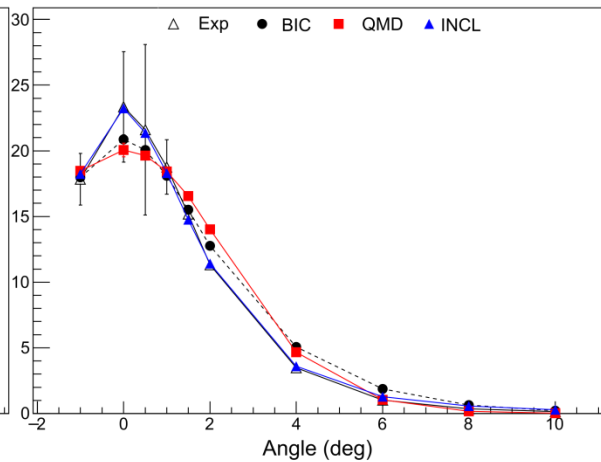
Angular Distribution

In total 32 distributions compared

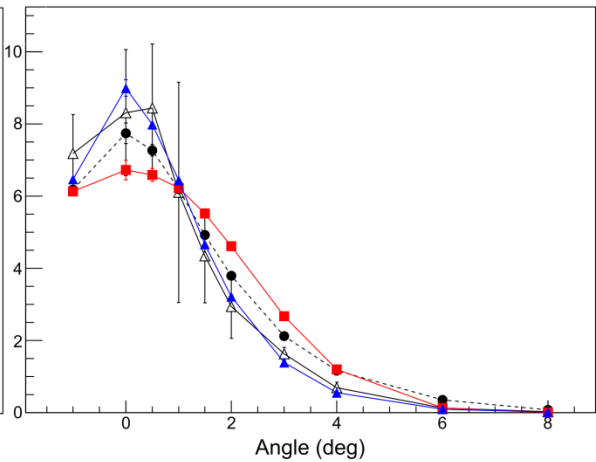
Thickness = 288mm, Z = 1



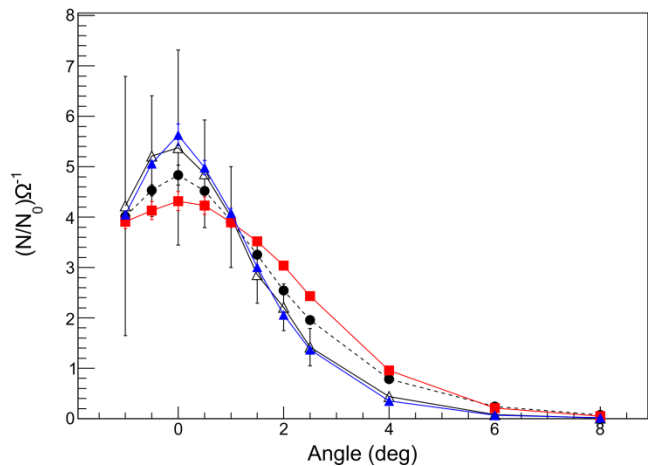
Thickness = 59mm, Z = 2



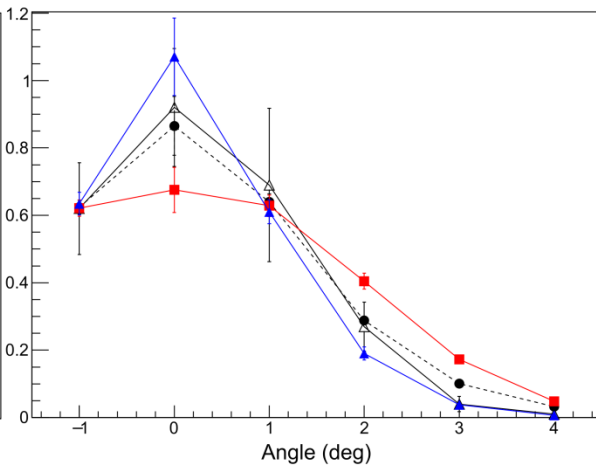
Thickness = 159mm, Z = 3



Thickness = 258mm, Z = 4

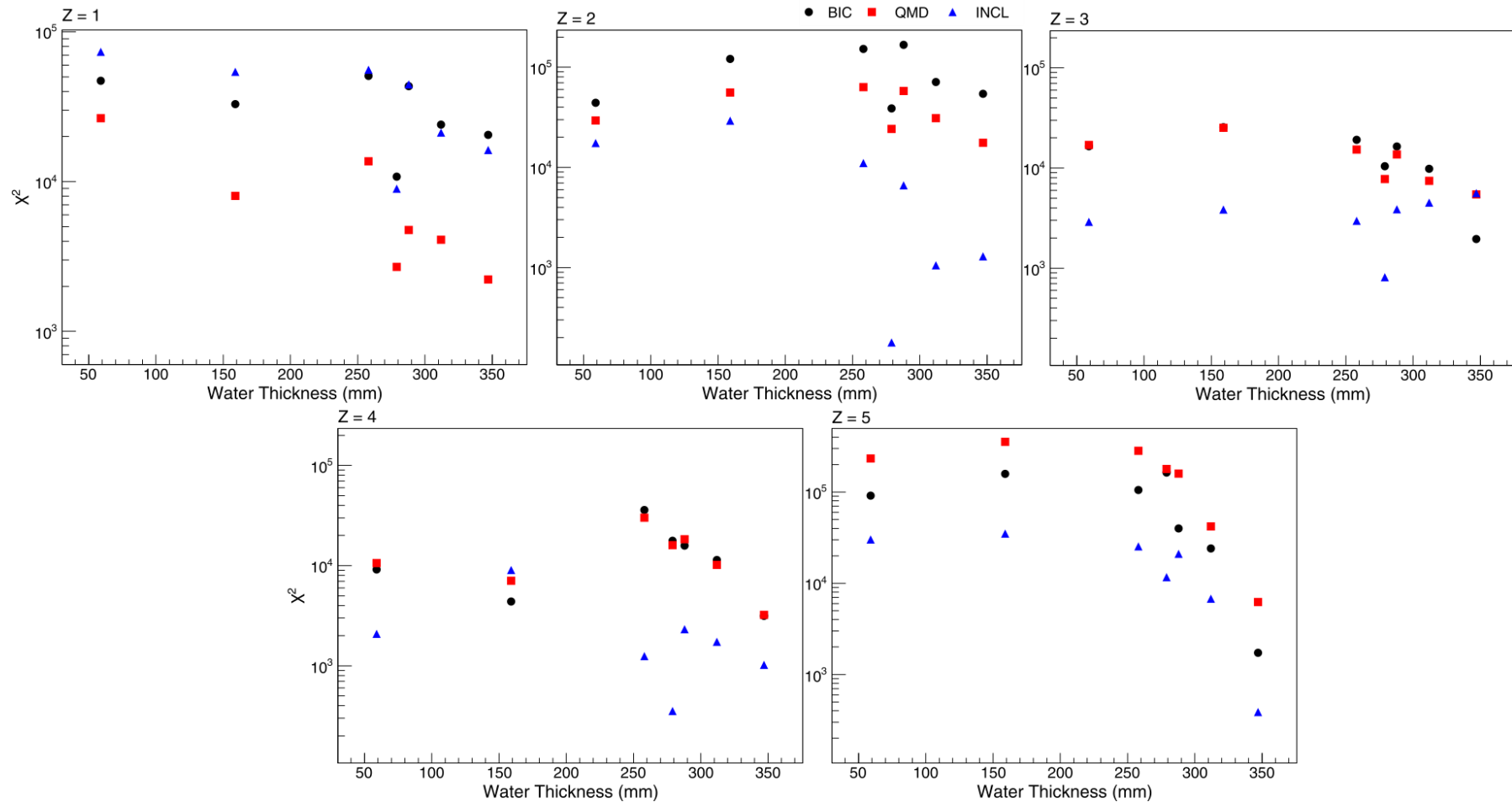


Thickness = 347mm, Z = 5



Be and B
have many
angles with an
error of more
than 40%

χ^2 values



Results: Angular Distribution

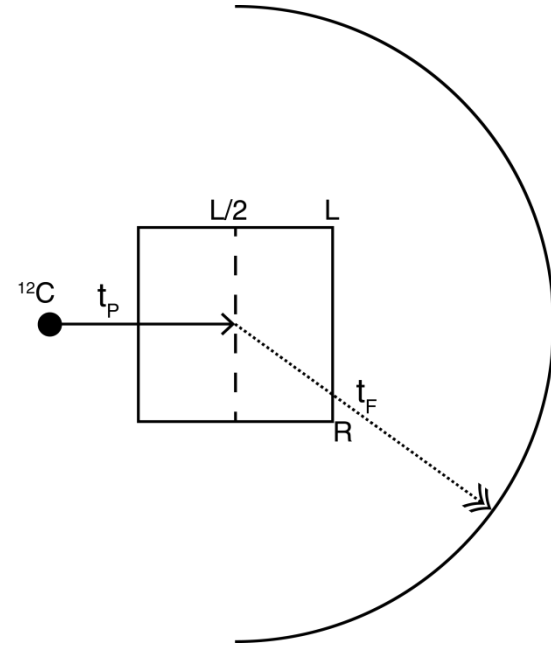
- INCL performs significantly better than the other models, particularly for higher Z
- QMD performs best for protons
- BIC and QMD produce broader distributions

Mean %Difference

Z	BIC	QMD	INCL
1	14 ± 4	7 ± 4	15 ± 4
2	24 ± 2	16 ± 2	7 ± 2
3	29 ± 8	26 ± 8	16 ± 8
4	47 ± 14	42 ± 14	18 ± 14
5	132 ± 12	135 ± 12	28 ± 13

Kinetic energy distributions

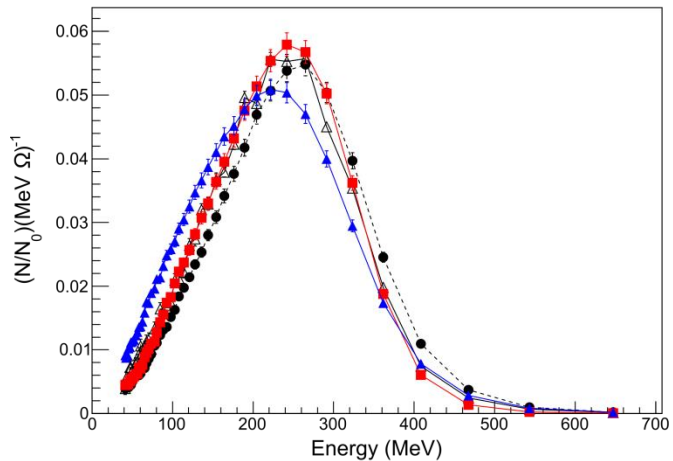
- Energy distributions calculated based on the time to reach the collection hemisphere
 - Same method adopted in the experimental measurements
- Assumptions :
 - All fragments are created at the centre of the phantom
 - Recorded fragments are due to the only most abundant isotope (^1H , ^4He , ^7Li , ^9Be , ^{11}B)



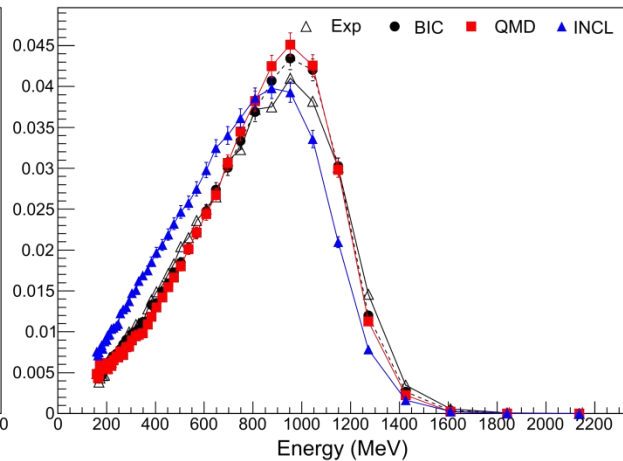
$$KE_F = \left(\frac{1}{\sqrt{1 - \beta^2}} - 1 \right) m_0 c^2$$

$$\beta = \frac{R}{ct_F}$$

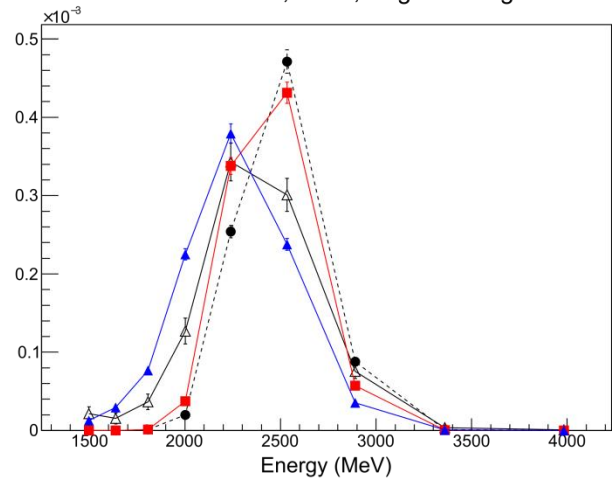
Thickness = 258mm, Z = 1, Angle = 4deg



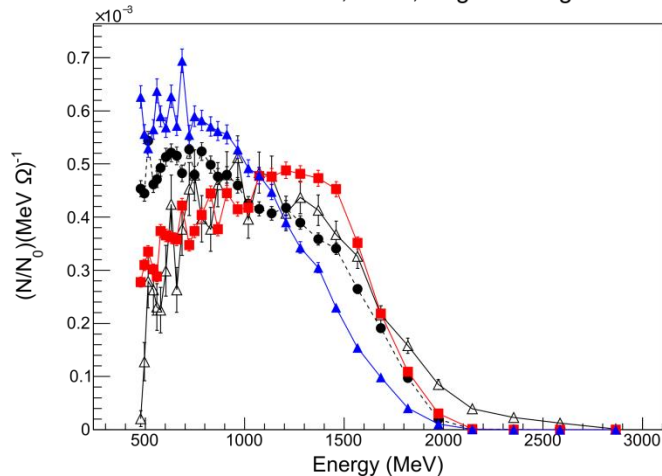
Thickness = 312mm, Z = 2, Angle = 1deg



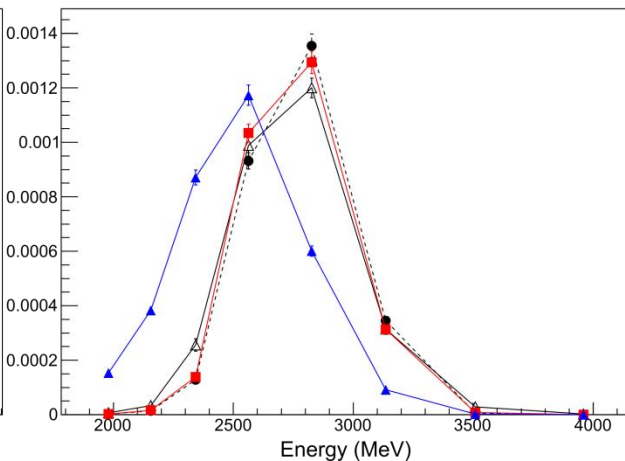
Thickness = 59mm, Z = 3, Angle = 4deg



Thickness = 347mm, Z = 4, Angle = 2deg

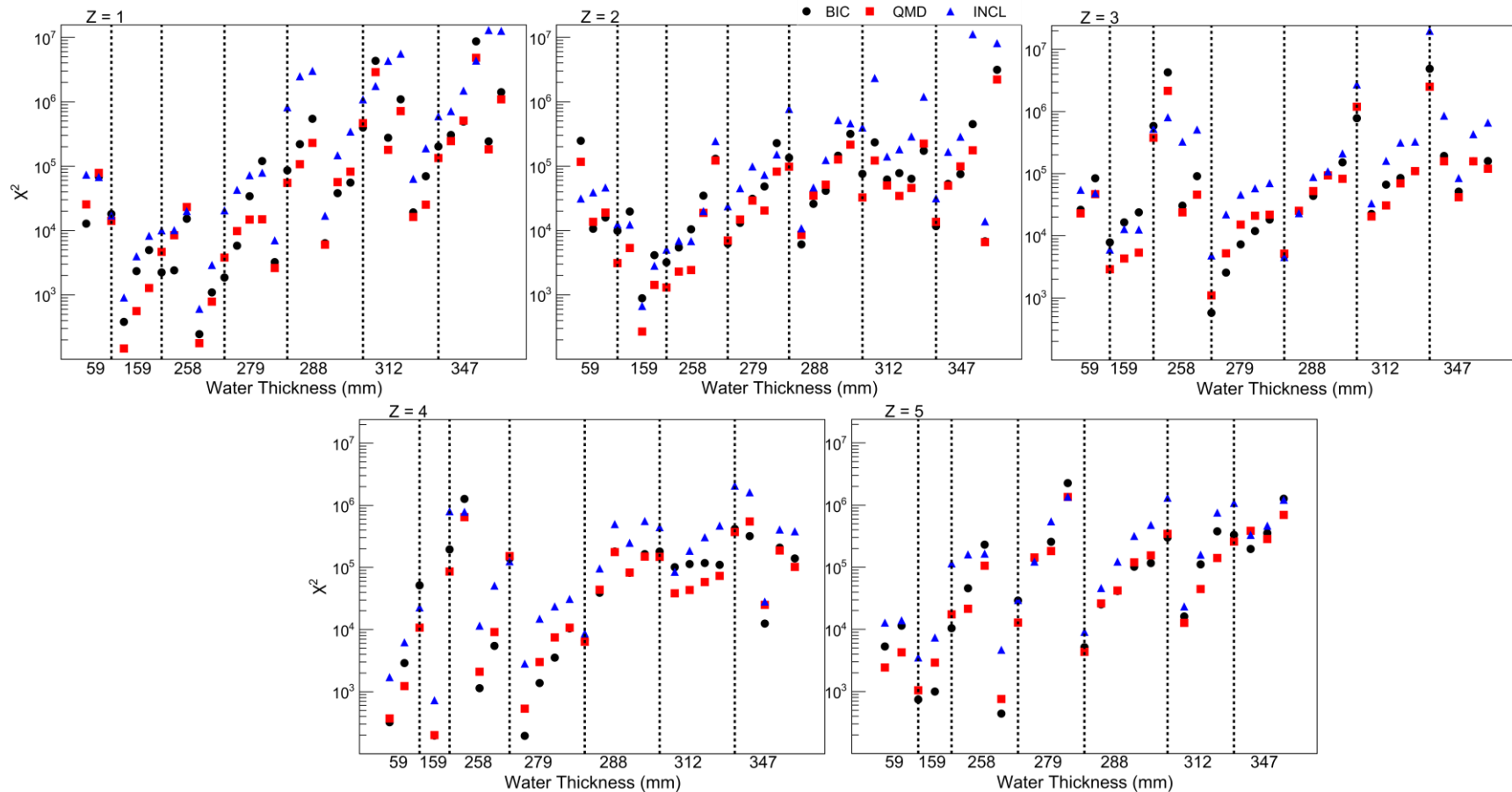


Thickness = 159mm, Z = 5, Angle = 3deg



Exp errors up
to ~20%

χ^2 values



Results: Energy Distributions

- BIC and QMD perform similar to one another with INCL performing noticeably more poor
- INCL commonly produces lower energy distributions
- Possible energy miscalibration of experiment may contribute to poorer agreement
 - Measurements done over two session
 - Calculated kinetic energy of the ^{12}C ion beam shifts from lower to higher energies
 - Results improving only for INCL by ~10%

Mean %Error

Z	BIC	QMD	INCL
1	26 ± 6	22 ± 6	46 ± 6
2	30 ± 7	33 ± 7	73 ± 7
3	41 ± 8	42 ± 8	93 ± 8
4	61 ± 9	52 ± 9	116 ± 9
5	221 ± 11	194 ± 10	398 ± 10

Comparison of execution times

- Comparison of execution times of 10^5 primary particles for each model
- Intel Xeon E5-2650v3 @2.30GHz
- QMD/QMD-F is considerably more computationally intensive
- BIC and INCL have similar execution times

Thickness	BIC (seconds)	QMD/BIC	QMD-F/BIC	INCL/BIC
59	97.5 ± 3.3	10.83 ± 0.45	7.73 ± 0.29	0.79 ± 0.05
159	569 ± 18.2	5.40 ± 0.18	3.94 ± 0.14	0.97 ± 0.03
258	1382.9 ± 90.7	3.67 ± 0.25	2.85 ± 0.24	1.04 ± 0.06
279	1643.4 ± 57.9	3.41 ± 0.15	2.46 ± 0.31	1.03 ± 0.12
288	1765 ± 63.6	3.29 ± 0.13	2.11 ± 0.22	1.01 ± 0.10
312	1979.1 ± 73.9	3.16 ± 0.13	2.26 ± 0.13	1.03 ± 0.05
347	2380.3 ± 47.6	2.86 ± 0.06	2.17 ± 0.08	1.00 ± 0.04

Summary

- Fragment data from a 400MeV/u ^{12}C beam in water was used to benchmark Geant4 using version 10.2p2
- **Fragment yield** values agreed within ~5-35% of experimental values
 - QMD-F best for H and He, BIC/QMD for heavier fragments
- **Angular Distributions** agreed ~7-30% for INCL, which performed much better than BIC and QMD
- **Energy distributions** agreed noticeably poorer (possible experimental calibration error)
 - BIC and QMD performed similar for angular and energy distributions (both treat interaction as Gaussian wave functions)
 - INCL produced lower energies
- In general the agreement deteriorates with larger fragments
- **Computation times** showed QMD considerably more intensive, BIC and INCL are similar

Conclusions

- Which model for Geant4 fragmentation?
 - Maybe QMD/ QMD-F
 - Repeat simulation with all alternative models and see the range of variation of the results
- The test will be part of the regression testing of Geant4 performed at SLAC and CERN
- As next developments, include
 - INCL-ABLA
 - Abrasion-Ablation model of Wilson
- There is the need of systematic validation against sets of exp data
 - Of different research groups
 - With different detectors
 - With increased experimental accuracy



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